## MATH 121 Functions—Functional Notation

1. (Section 1.2) If g(x) = -2x+7, find and simplify completely: a) g(0) b) g(1) c) g(-2) d) g(4)e) g(a) f)  $g(\bigcirc)$  g) g(x+h)2. (Section 1.2) If  $f(x) = \frac{x^2-2}{x+2}$ , find and simplify completely: a) f(1) b) f(-1) c) f(0) d) f(-3)

e) 
$$f(a)$$
 f)  $f(\odot)$  g)  $f(x+h)$ 

3. (Section 1.2) Suppose *f* is the function given by  $f(x) = -x^2 + 2x - 5$ . Simplify each of the following completely.

a) 
$$\frac{f(x+h)-f(x)}{ax}$$
 b)  $\frac{f(w)-f(1)}{1-w}$  c)  $\frac{f(-2)}{3} + \frac{f(6)}{2}$   
d)  $\frac{f(x^2)-f(2x)}{xf(x)}$  e)  $\frac{f(x+1)-f(x-1)}{2x}$ 

4. (Section 1.2, 2.2) Let g be the function given by  $g(x) = \frac{2}{x}$ . Find and simplify: g(2+h) - g(2)

$$\frac{g(2+h)-g(2)}{h}$$

5. (Section 1.3, 1.4) For a linear function f, f(2) = 4 and f(-1) = 3.

- a) Find the function.
- b) Find f(3).
- c) For what x is f(x) = -100?

6. (Section 1.3, 1.4) Suppose f is a <u>linear</u> function, and it is known that f(-1)=2 and f(2)=-5.

- (a) Find f(9).
- (b) For what input x is  $f(x) = \frac{35}{4}$ ?

7. (Section 1.3, 1.4) For a linear function f, f(-1) = 3 and f(2) = 5.

- a) Find a formula for f(x).
- b) Write two other points for this function.
- c) Determine the intercepts of the graph of f.

- d) Determine the exact value of f(7.5).
- e) For what x is  $f(x) = -10\frac{3}{5}$ ?

8. (Section 2.2) Consider the functions  $p(x) = -x^2$  and  $q(x) = \sqrt{19 - 3x}$ 

a) What is the domain of q?

b) Simplify completely: 
$$-4 \cdot p(-4)$$

c) Simplify completely: 
$$\sqrt{\frac{q(5)}{5-p(-2)}}$$

d) Simplify completely: 
$$[q(-2)-q(-10)]^2$$

e) Simplify completely: 
$$\frac{p(6)+6}{p(2)+2}$$

f) Simplify completely: 
$$\frac{p(x+h) - p(x)}{2h}$$

9. (Section 2.3) Suppose p is the function  $p(x) = 2x + \frac{20}{x} - 5$ .

- (a) For what input(s) x is p(x) = 8?
- (b) For what input(s) x is p(x) = 36?
- (c) Solve the following equation: p(2x) = p(x)

10. (Section 2.3) Suppose *f* and *g* are the functions given by f(x) = x - 5 and  $g(x) = \frac{x-8}{x}$ . Solve each of the following equations.

a) 
$$f(x) + g(x) = f(8)$$

b) 
$$f(2x+1)-f(3-x)=g(-6)$$

c) 
$$g(-4) \cdot g(x+8) = g(-8) \cdot g(-x+8)$$

11. (Section 3.5) Suppose f is the function  $f(x) = 3 - \frac{1}{3}x$  and g is the function g(x) = -x + 4. Solve for x in each of the following equations.

(a) 
$$|f(x)+2| = \frac{g(-2)}{2}$$

(b) 
$$5 - \frac{6|g(x)|}{5} = f(0)$$
  
(c)  $|f(2x)| = |g(-x)|$ 

12. (Section 5.1) Let  $f(x) = 3 + x + x^3$ ,

- a. Find  $f^{-1}(5)$
- b. Graph f by plotting points.
- c. Graph  $f^{-1}$ ; comment on the relationship between the graph of f,  $f^{-1}$ , and y = x.

13. (Section 4.6) Let  $f(x) = \frac{x-4}{2x^3 - x^2 - 8x + 4}$ 

- a. Find all x such that f(x) > 0.
- b. Find all x such that f(x) < -1.

14. (Section 4.5) Let  $f(x) = \frac{x^2}{x-1} + 1$  and  $g(x) = \frac{4x-2}{x-2} + \frac{x+4}{2}$ 

- a) Find the *x*-intercepts of the graph of *f*.
- b) Find the *x*-intercepts of the graph of *g*.
- c) Find the value(s) for x, if any exist, for which f(x) = g(x).

15. (Section 4.6) Suppose f and g are functions such that  $f(x) = \frac{x-5}{2} - \frac{3x-1}{4}$  and  $g(x) = \frac{1}{3} - \frac{3}{5}x$ , solve each of the following:

- a) f(0) > g(x)
- b)  $f(x) \le g\left(\frac{-5}{3}\right)$

16. (Section 4.5) Let  $f(x) = \frac{x}{x-2}$  and  $g(x) = x^2 + 3$ . Find and simplify completely:

a) 
$$\frac{(g \circ f)(3)}{(f \circ g)(3)}$$
 b)  $\frac{g(x+2)-g(x)}{x \cdot g(1)}$ 

## 17. (Section 5.1)

a) Let f be a function such that f(2) = 4 and f(8) = 0. If g is the inverse function of f, find and simplify:  $\frac{(f \circ g)(4)}{g(0)} + (g \circ f)(1)$ 

b) Find the inverse of the function:  $f(x) = \sqrt[3]{\frac{4+3x}{x}}$ 

18. (Section 5.1) Suppose f and g are one – to – one functions such that f(2) = 7, f(4) = 2, and g(2) = 5. Find the value, if possible, of

a)  $(g \circ f^{-1})(7)$ b)  $(f \circ g^{-1})(5)$ c)  $(f^{-1} \circ g^{-1})(5)$ d)  $(g^{-1} \circ f^{-1})(2)$ e)  $(f \circ f^{-1})(7)$ f)  $(f^{-1} \circ f)(8)$ g)  $(g \circ g)(2)$ 

## **Answer Keys:**

1. (a) 7 (b) 5 (c) 11 (d) -1 (e) -2a + 7 (f) -2 
$$\odot$$
 + 7 (g) -2(x + h) + 7  
2. (a)  $\frac{-1}{3}$  (b) -1 (c) -1 (d) -7 (e)  $\frac{a^2 - 2}{a + 2}$  (f) ( $\odot^2 - 2$ )/( $\odot$  + 2)  
(g)  $\frac{(x+h)^2 - 2}{(x+h) + 2}$   
3. (a)  $\frac{-2xh - h^2 + 2h}{ax}$  (b) w - 1 (c) 11 (d)  $\frac{x^3 - 6x + 4}{x^2 - 2x + 5}$   
(e)  $\frac{-2x + 2}{x}$   
4.  $\frac{-1}{2+h}$   
5. (a)  $y = \frac{x}{3} + \frac{10}{3}$  (b)  $\frac{13}{3}$  (c) -310  
6. (a)  $f(9) = 12$  (b)  $x = \frac{47}{4}$   
7. (a)  $f(x) = \frac{2}{3}x + \frac{11}{3}$  (b)  $\left(0, \frac{11}{3}\right)$ ,  $\left(1, \frac{13}{3}\right)$  (c)  $\left(0, \frac{11}{3}\right)$ ,  $\left(-\frac{-11}{2}, 0\right)$ 



